Solution:

Consider the graph with $s = 1$ and arc-costs as shown. There is a unique shortest path from $s$ to $1$, and from $s$ to $2$, and the union of these is not a tree.

(Of course, the graph contains a negative cycle)